

Cosmological Constraints from the Cluster Baryon Mass Function

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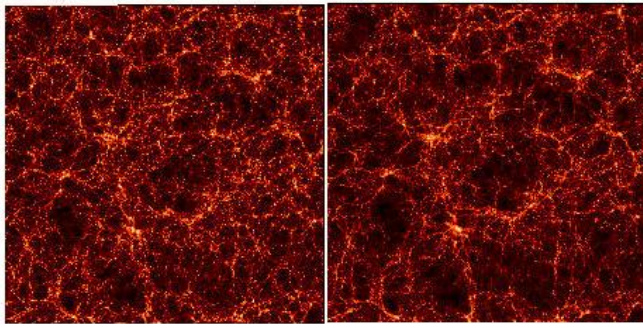
Clusters and cosmology

	Ω	Λ	h	σ_8
SCDM:	1	0	0.5	0.51
Λ CDM:	0.3	0.7	0.7	0.9
OCDM:	0.3	0	0.7	0.85
τ CDM:	1	0	0.5	0.51

$z=0$

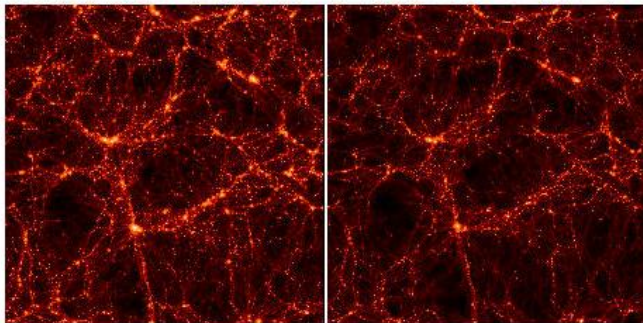
SCDM

τ CDM



Λ CDM

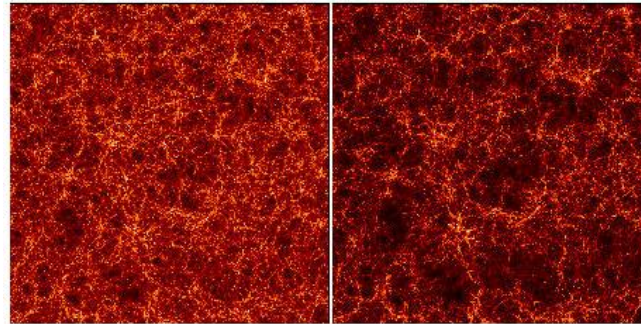
OCDM



$z=1$

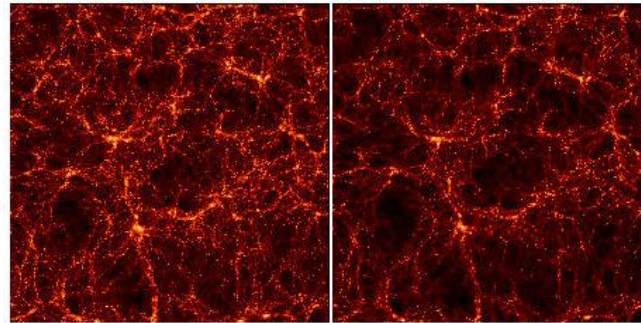
SCDM

τ CDM



Λ CDM

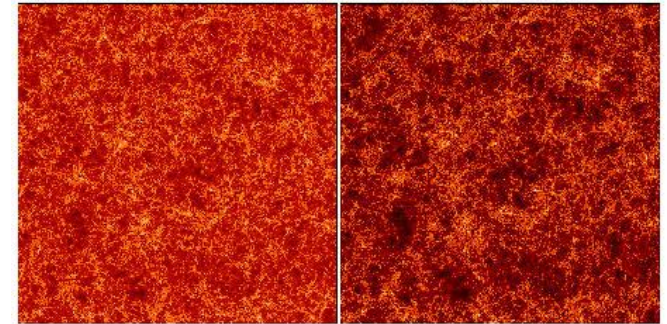
OCDM



$z=3$

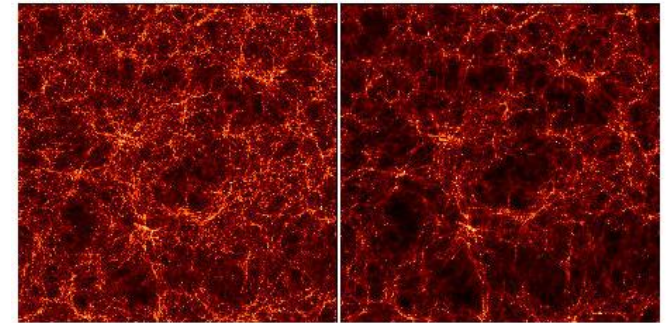
SCDM

τ CDM



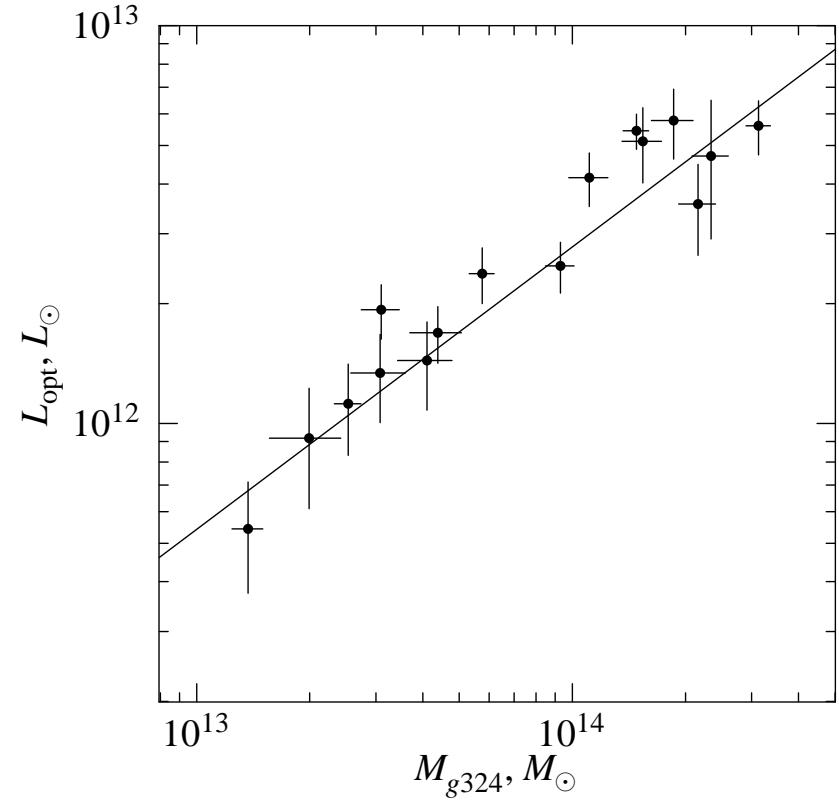
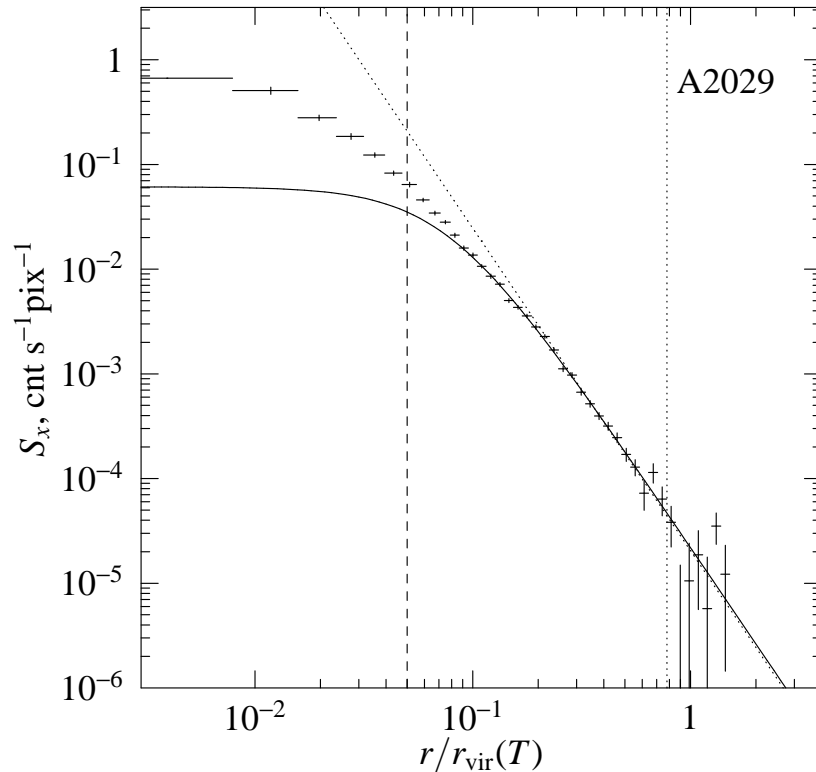
Λ CDM

OCDM



M_b as a proxy for M_{tot}

- $f_b = \frac{M_b}{M_{\text{tot}}} = \frac{\Omega_b}{\Omega}$ — (almost) independent of cluster mass or redshift. — *Steve Allen's talk*
- M_b is easily and directly measured at $r \sim r_{\text{vir}}$:



✓ X-ray imaging (*ROSAT*) provides surface brightness (gas mass profile) to $r \sim r_{\text{vir}}$.

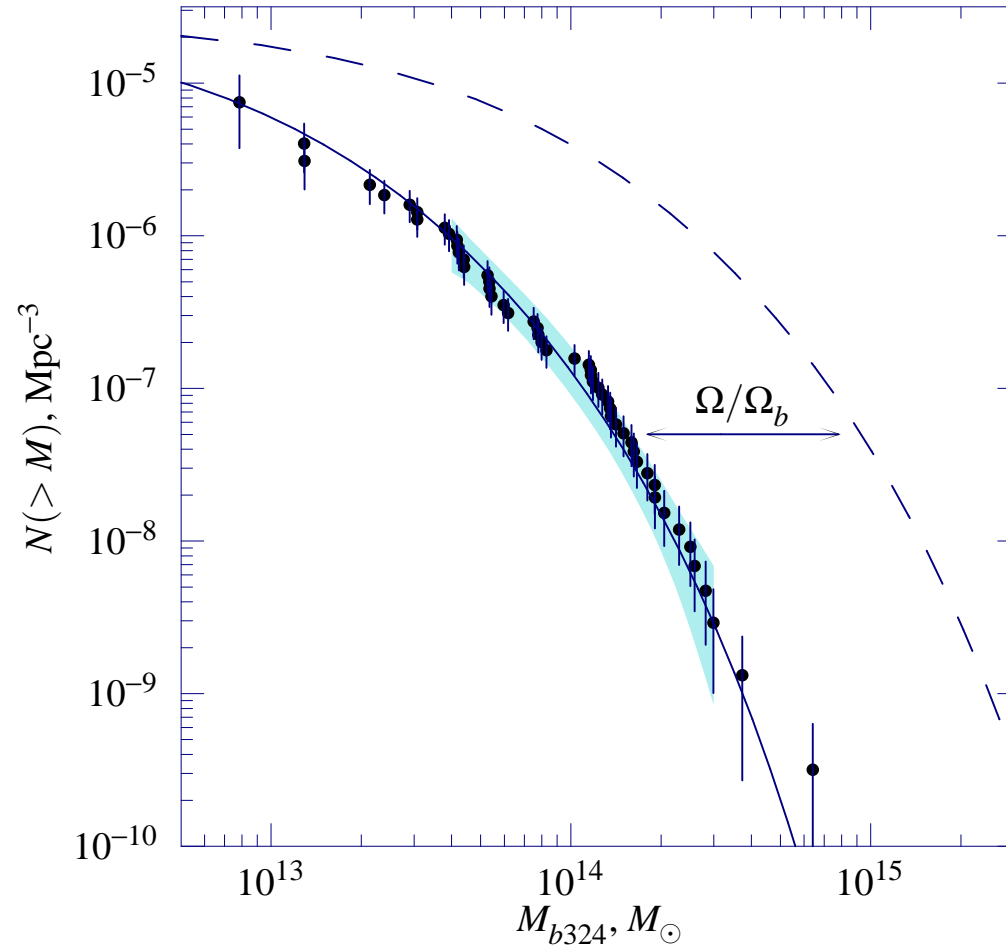
✓ $\frac{M_b}{M_g} = 1.100 + 0.045 \left(\frac{M_g}{10^{15} M_{\odot}} \right)^{-0.5}$

✓ $\delta_b = \delta_M \implies r_{\delta}$ can be estimated from the X-ray imaging alone

- **Cluster baryon mass functions are easily and directly measured.**

@ $z = 0$ (HIFLUGCS sample):

Voevodkin & Vikhlinin astro-ph/0305549



- **Absolute measurements of f_b not needed to fit cosmology:**

✓ Ω_b known from BBN: $\Omega_b h^2 = 0.020$ (Burles et al.) or WMAP $\Omega_b h^2 = 0.0224 \pm 0.001$.

✓ Models for the total mass function computed assuming an Ω_M , this fixes the scaling between a model for $F_{\text{tot}}(M_{\text{tot}})$ and measurements of $F_b(M_b)$: $F_b(M_b) = F_{\text{tot}}(\Omega/\Omega_b M_b)$.

- **See Voevodkin & Vikhlinin astro-ph/0305549 for results on σ_8 and $\Omega_M h$.**

Cluster evolution: high-z sample

160 deg² survey

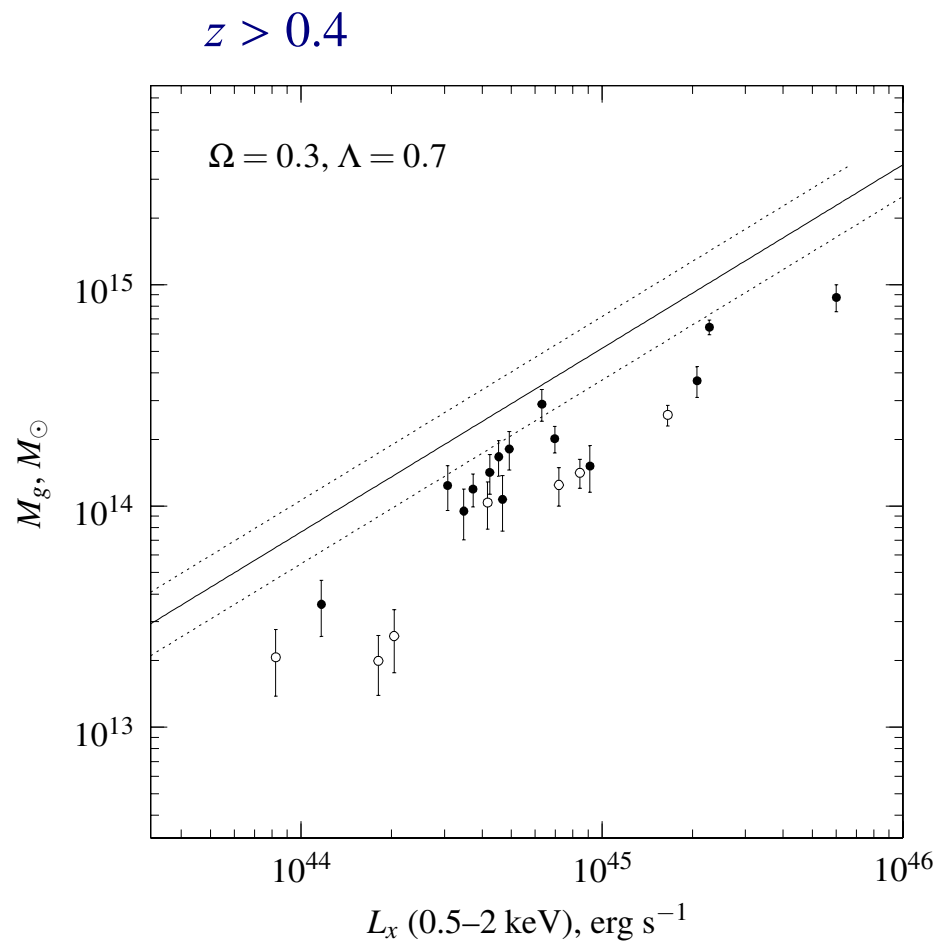
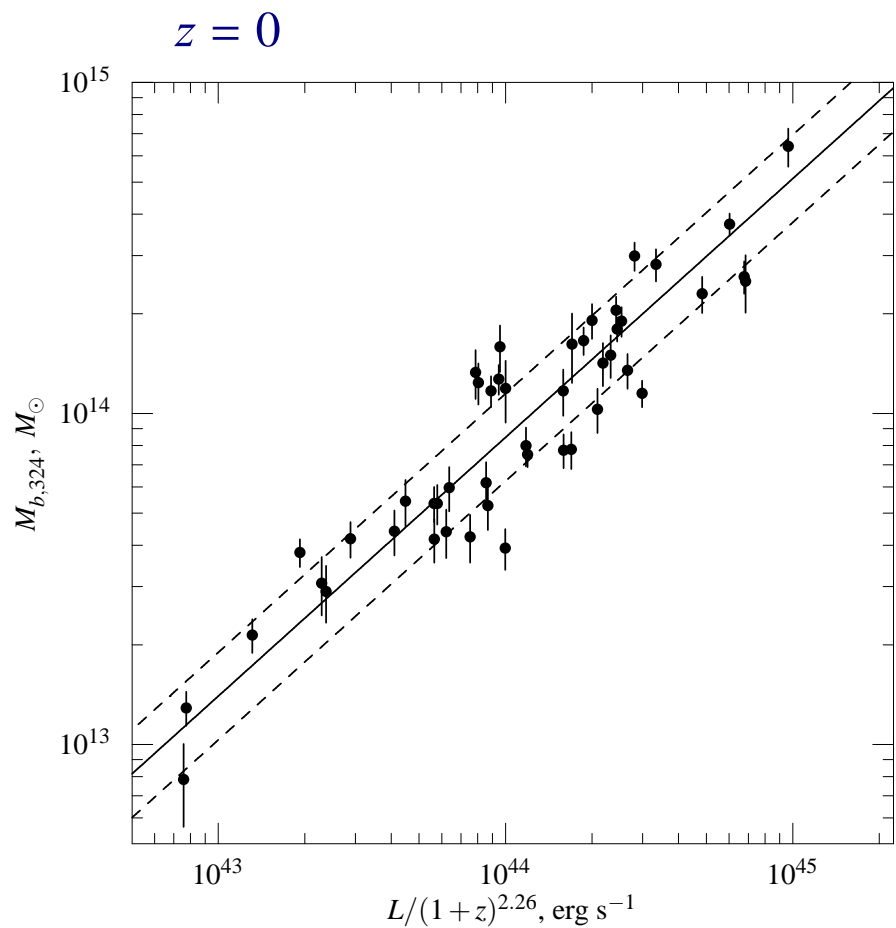
- Large area — 650 ROSAT PSPC pointings, 160 square degrees.
- 100% optically identified, fully published (Vikhlinin et al. 1998, Mullis et al. astro-ph/0305228)
- High quality:
 - Total sample 223 X-ray candidates, 201 optically confirmed as clusters
 - For $f_x > 1.4 \times 10^{-13}$ erg s⁻¹ cm⁻² 114 X-ray candidates, 111 confirmed as clusters
- X-ray fluxes are good: *Chandra* followup shows no bias within 5%.
- Survey area calibrated via extensive Monte-Carlo simulations.
- Large distant sample — 45 clusters at $z > 0.4$

Chandra followup

7 brightest clusters at $z > 0.4$ observed with long exposures (PIs L. VanSpeybroeck, S. S. Murray).

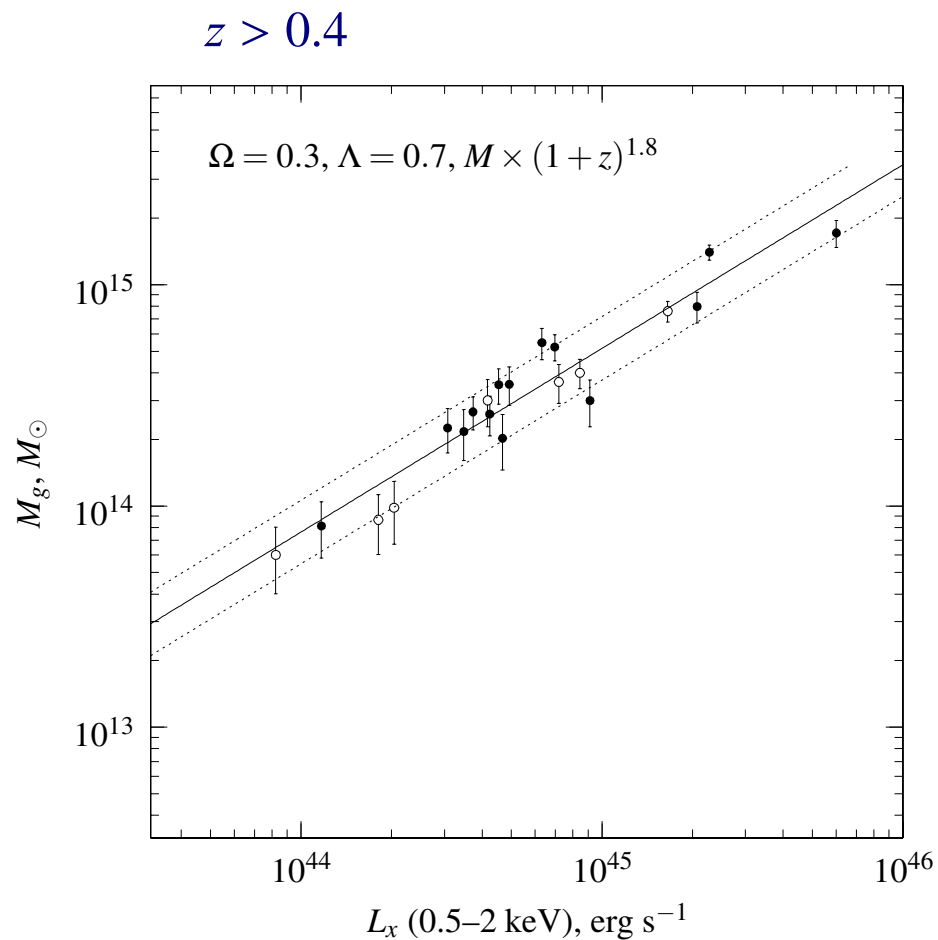
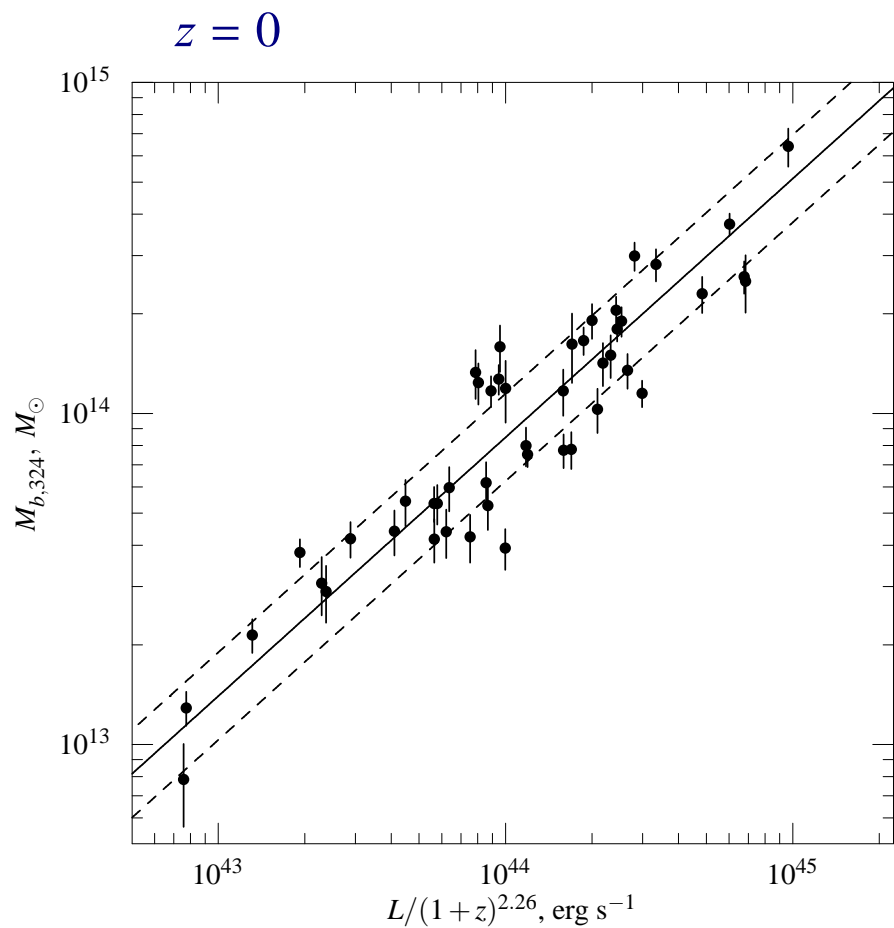
$$\Delta T/T \sim 10\%, \Delta M_g/M_g \sim 20\%$$

Cluster evolution: scaling relations at $z > 0.4$



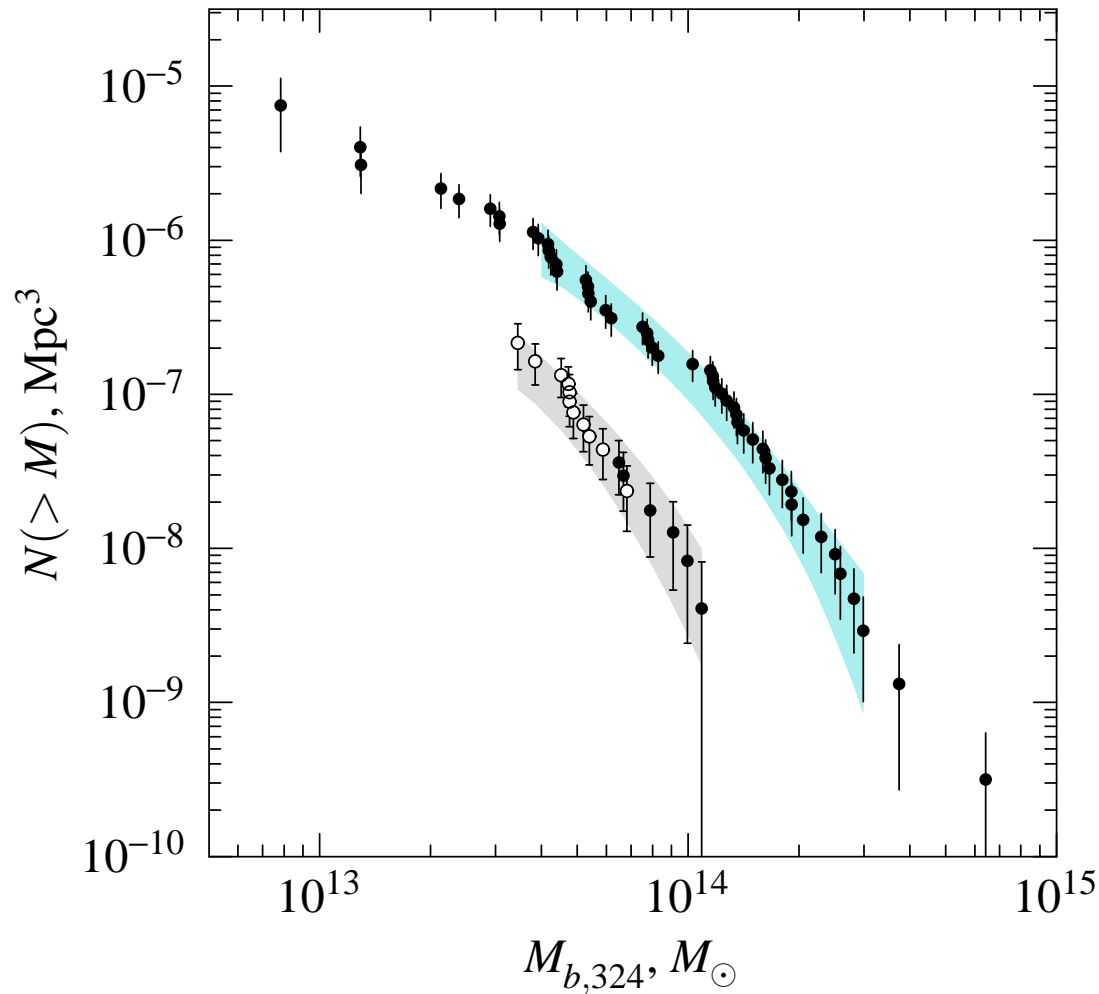
$M_b \propto (1+z)^{-1.8 \pm 0.4}$ — mass at a fixed L_x decreases with z .

Cluster evolution: scaling relations at $z > 0.4$



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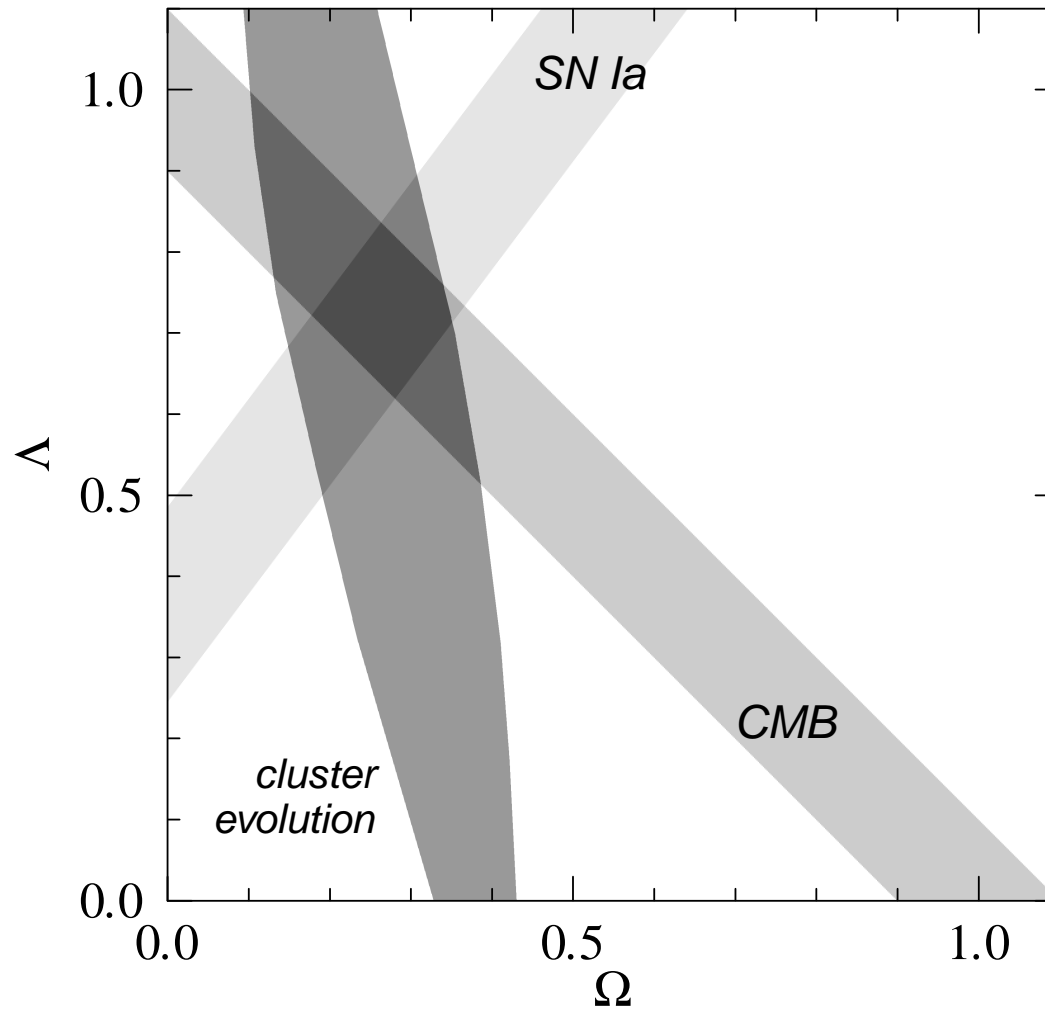
Evolution of the baryon mass function at $z > 0.4$



- Fix $\Omega_b h^2 = 0.0224$, $h = 0.71$, $n = 1$.
- Compute mass function models on a grid of Ω , Λ , and σ_8
- A pair of (Ω, Λ) is acceptable if model fits data at $z = 0$ and $z > 0.4$ for some σ_8 .

Cluster evolution constraints on Ω , Λ

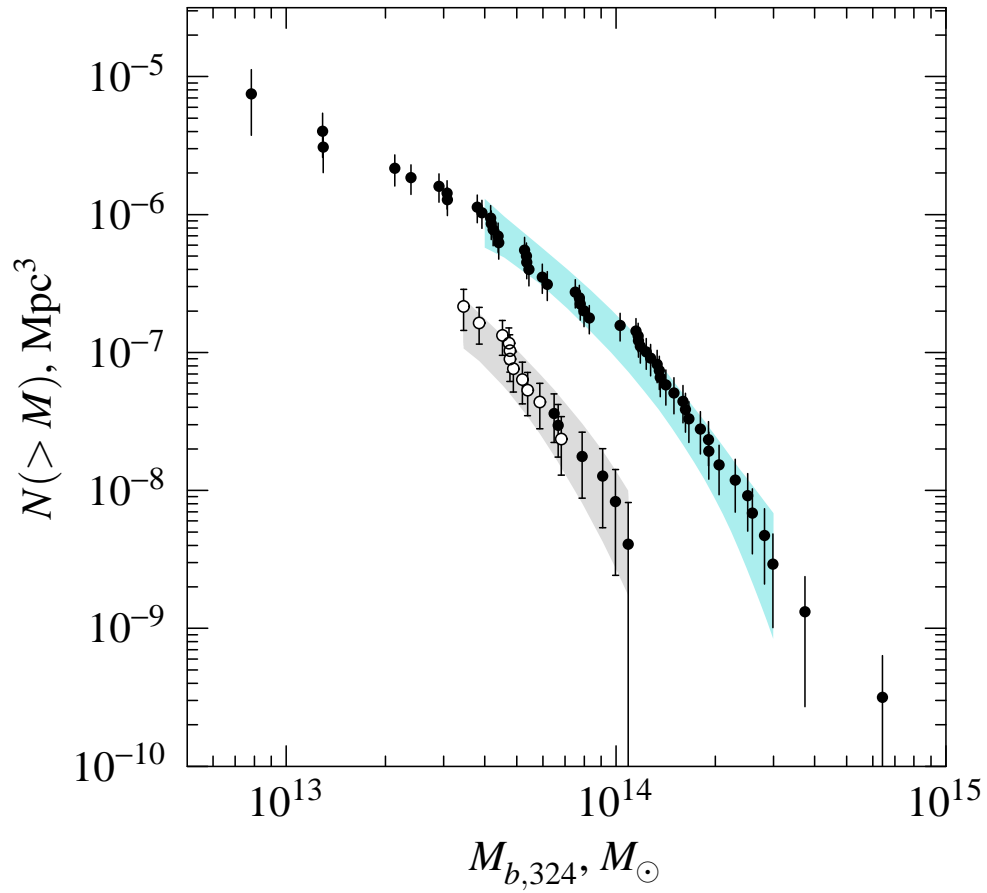
Vikhlinin et al. 2003 (astro-ph/0212075)





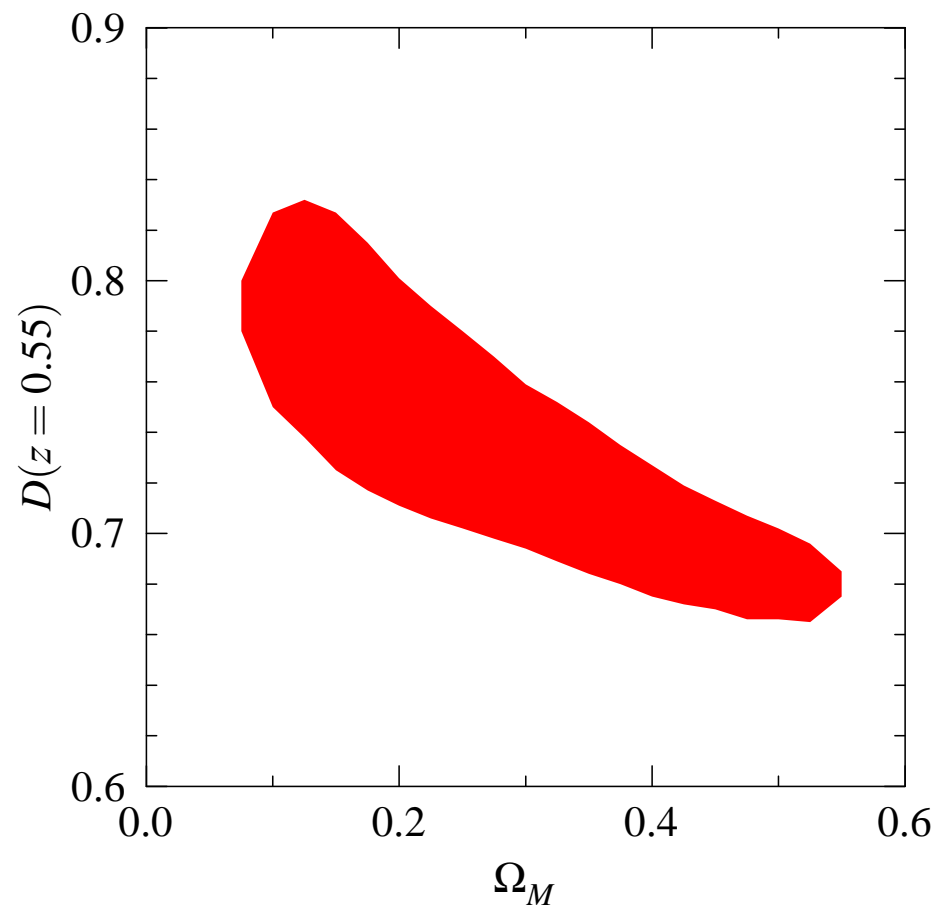
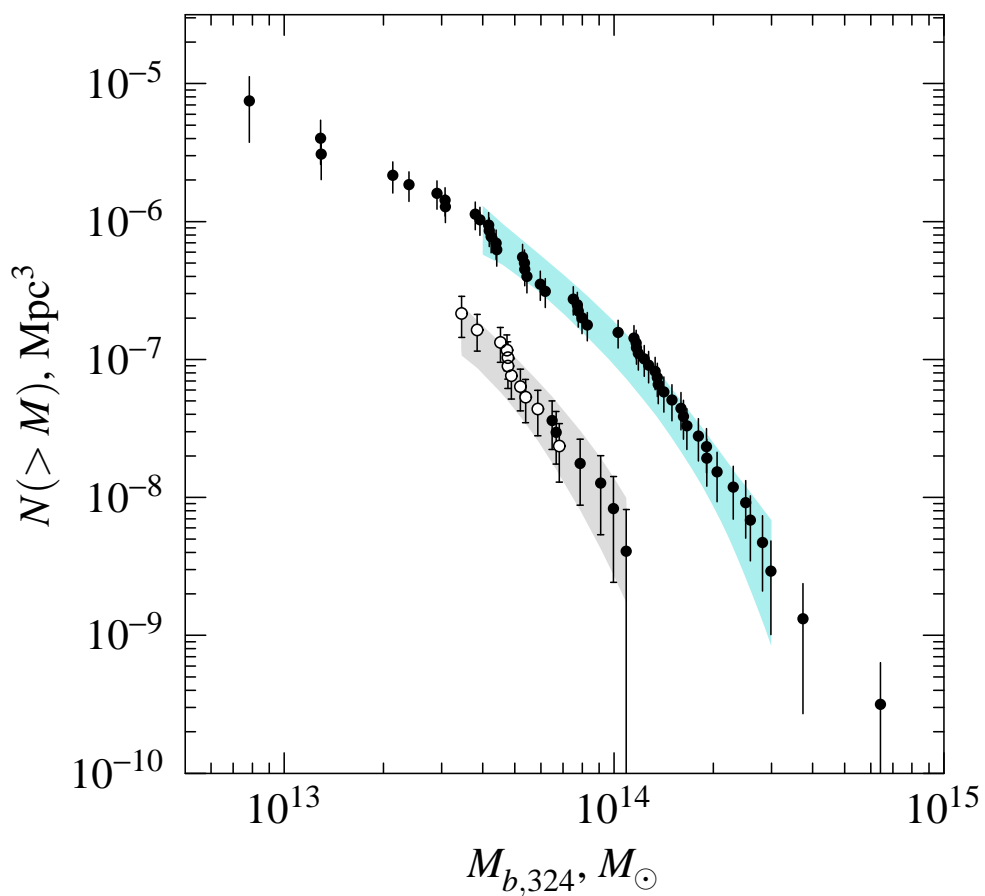
Growth factor and equation of state

Cluster evolution *really* constrains the growth factor for linear density perturbations $D(z)$:



Growth factor and equation of state

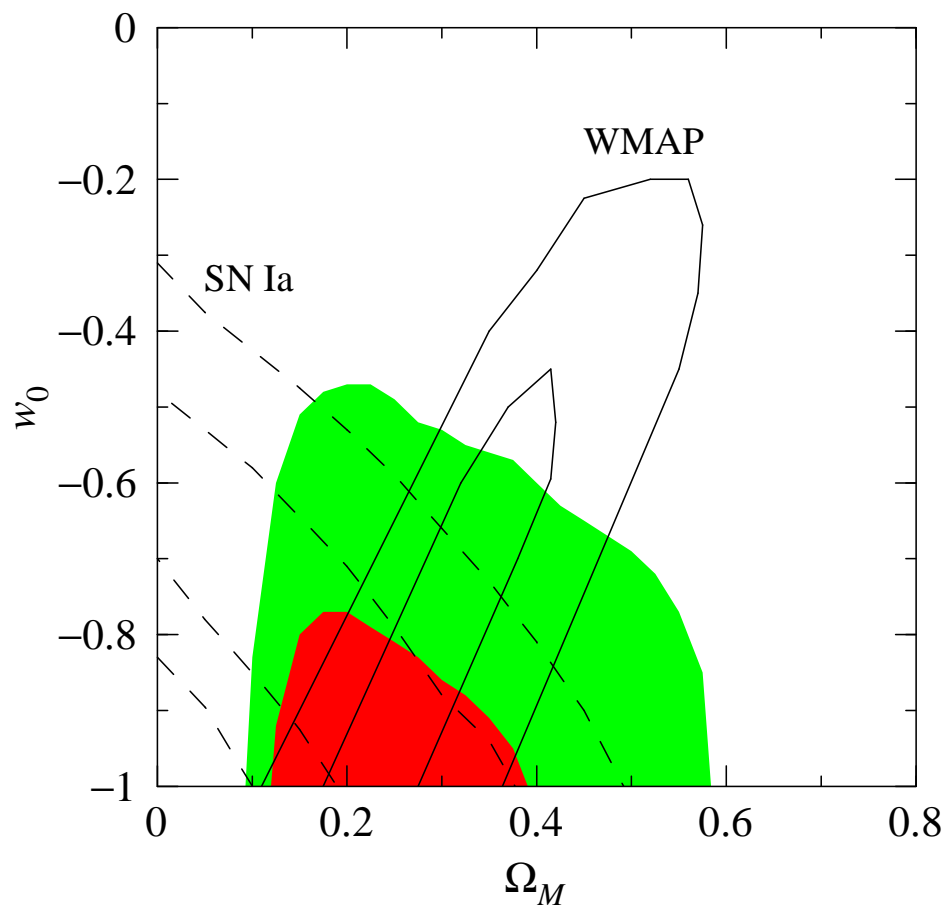
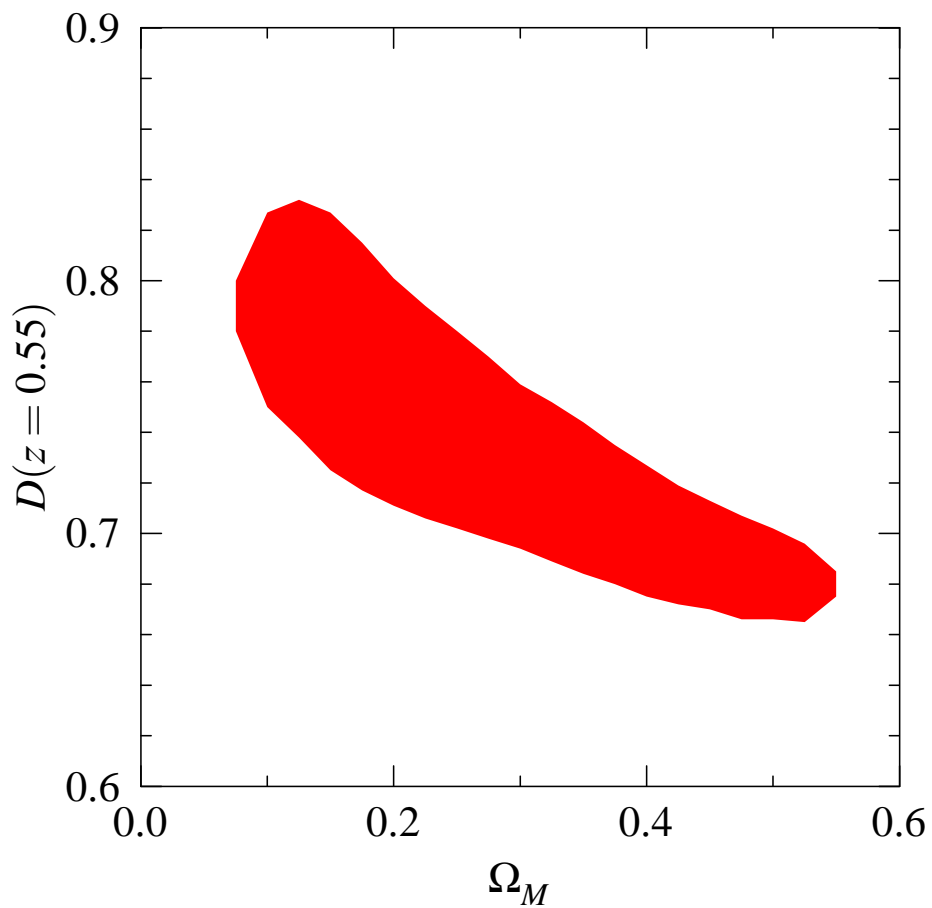
Cluster evolution *really* constrains the growth factor for linear density perturbations $D(z)$:



$$D(0.55) = 0.727 \pm 0.033 \text{ for } \Omega = 0.3$$

Growth factor and equation of state

Assuming flat Universe, $D(z)$ converts to w :



For $\Omega_M = 0.3$, $w < -0.86$ (68%), $w < -0.67$ (90%), $w < -0.5$ (95%)

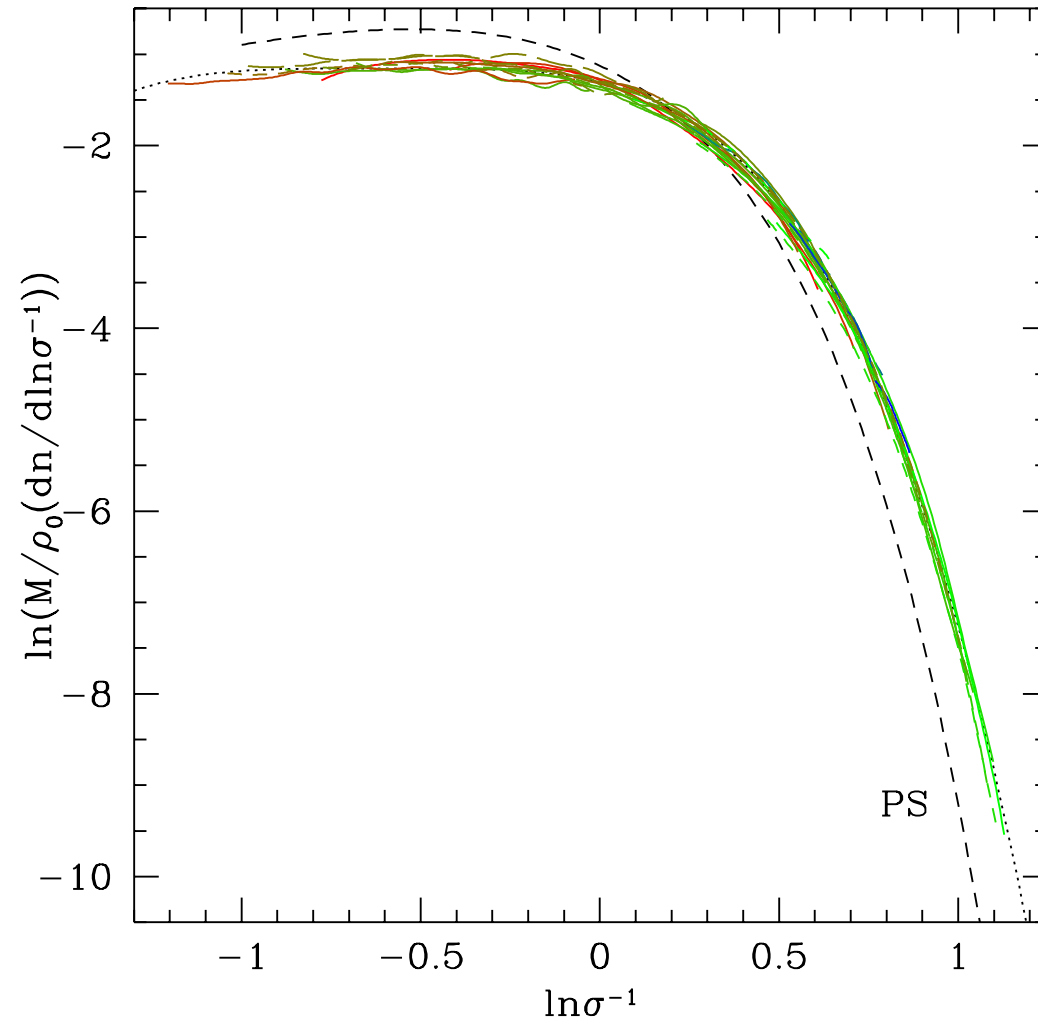
CONCLUSIONS

- Good samples from ROSAT to study local cluster population and evolution at $z = 0.4 - 0.7$ (~ 50 objects available).
- Evolution of scaling relations to $z \sim 0.5$ now directly observed by Chandra and XMM.
- Baryon mass function is a good proxy for the total mass function in clusters.
- Cluster evolution constraints on (Ω, Λ) (from 17 brightest $z > 0.4$ clusters in the 160 deg² survey) comparable in quality to SN Ia and pre-WMAP CMB results.
- Meaningful constraints on w (favor the cosmological constant, $w = -1$)

Theory for F(M)

- Jenkins et al., for M_{tot} at $\delta = 324$

$$\frac{M}{\langle \rho \rangle} \frac{dF(M)}{d \ln \sigma(M, z)^{-1}} = 0.316 \exp \left(- \left| \ln \sigma(M, z)^{-1} + 0.67 \right|^{3.82} \right)$$



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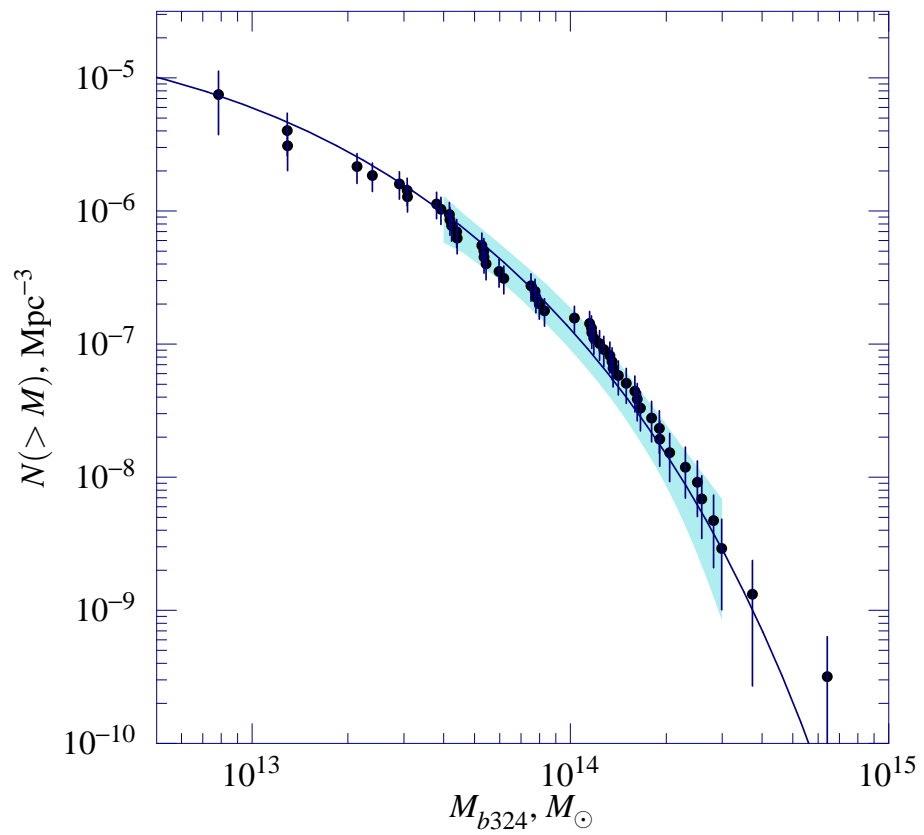
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- ✓ $\sigma(M, z) = \sigma_0(M) D(z)$
- ✓ $\sigma_0(M) \iff P(k) = k^n T^2(k)$, known for any $n, \Omega, h, \Omega_b, \sigma_8$ (analytical approximations for $T(k)$ in Eisenstein & Hu 1998)
- ✓ $D(z)$ known for any cosmology $\Omega, [\Lambda, [w \dots]]$.

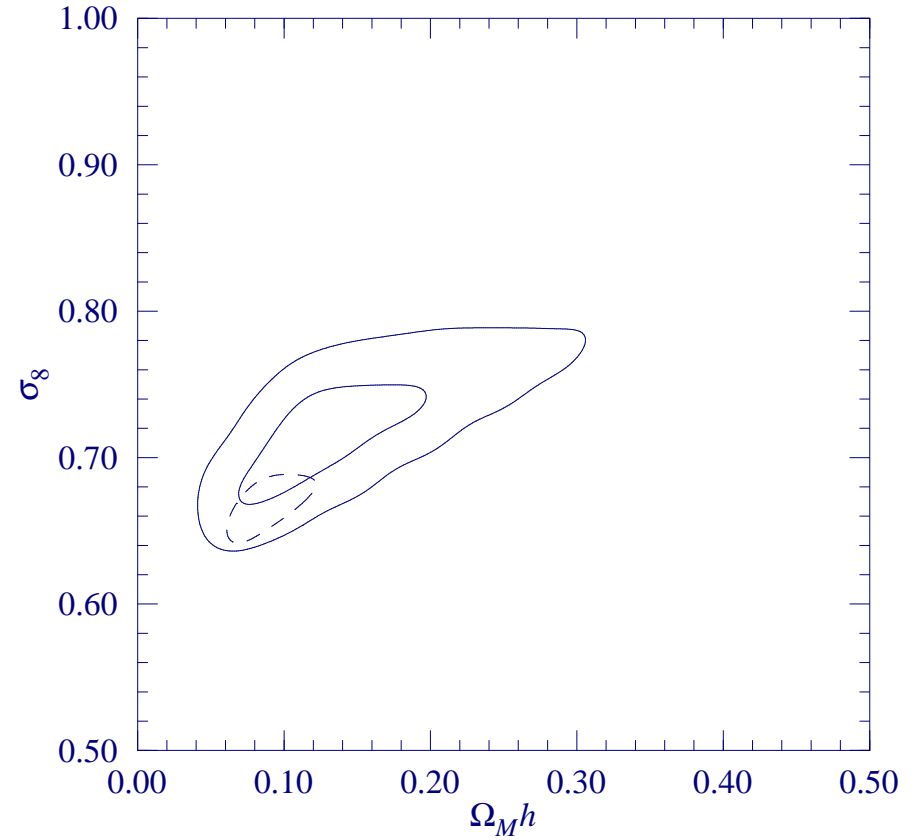
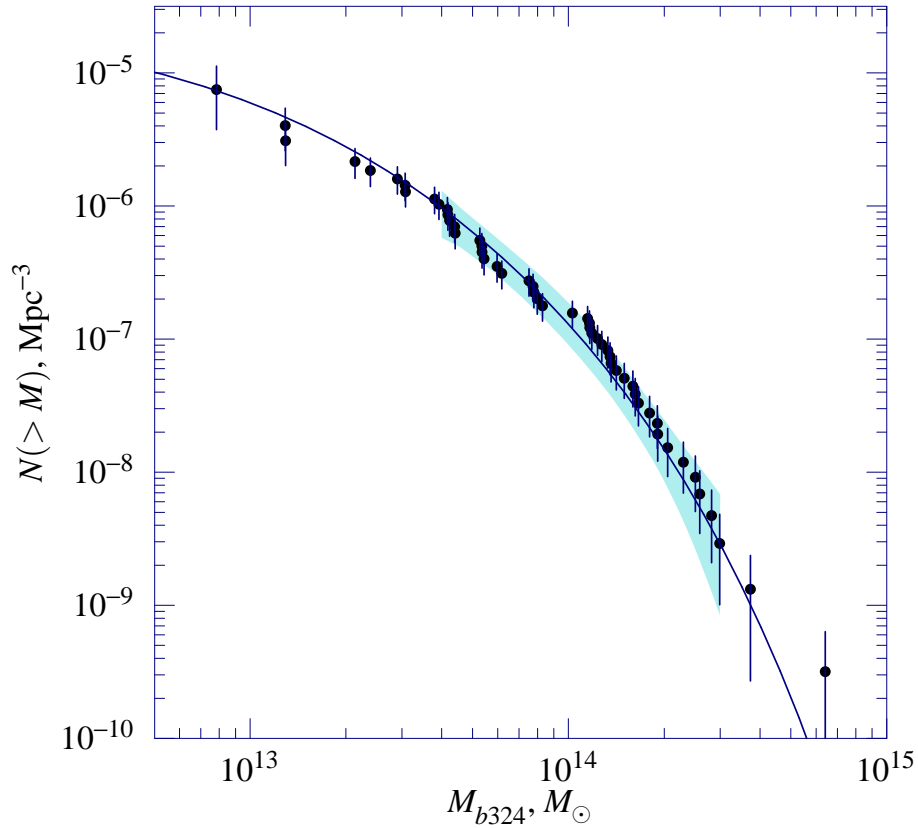
Results at $z=0$

Voevodkin & Vikhlinin (astro-ph/0305549)



Results at $z=0$

Voevodkin & Vikhlinin (*astro-ph/0305549*)



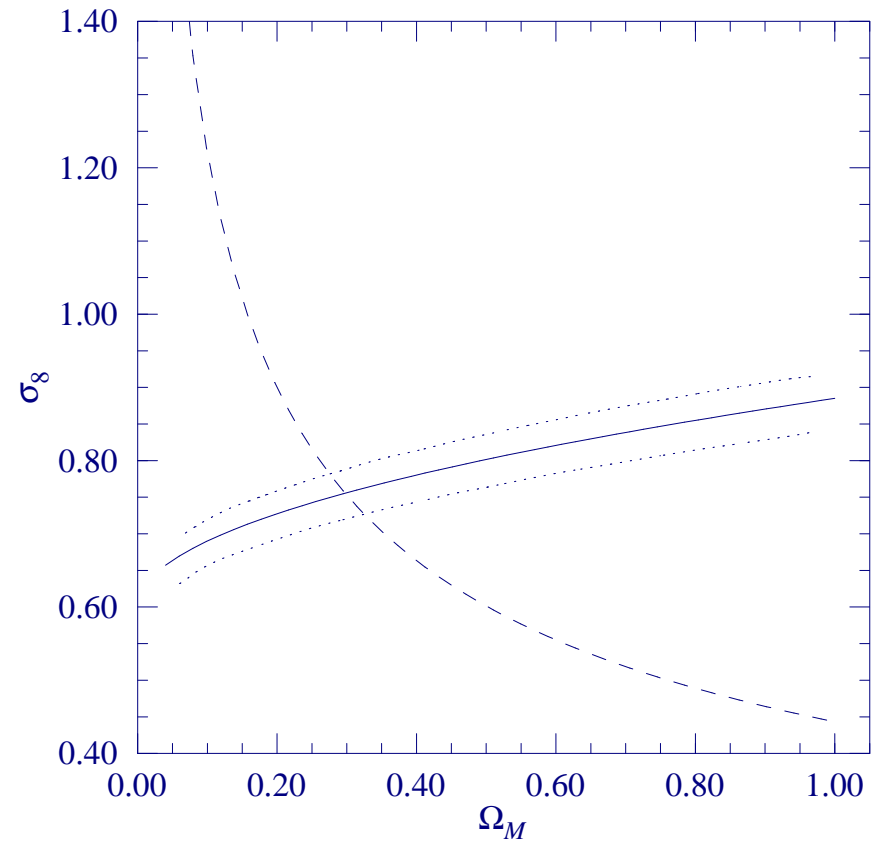
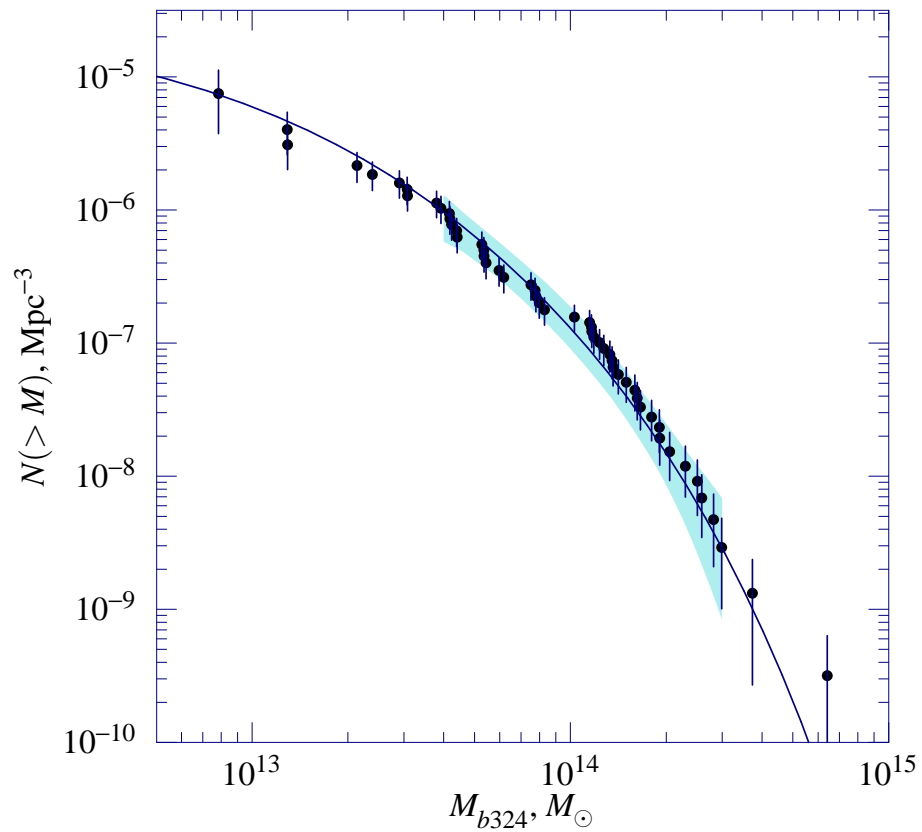
- $F(M)$ in a range of $4 \times 10^{13} M_\odot < M_b < 4 \times 10^{14} M_\odot$ constraints σ_8 and slope of $P(k)$:

$$\sigma_8 = 0.72 \pm 0.04 \quad \Omega_M h = 0.13 \pm 0.07 \quad (\Omega_M = 0.18 \pm 0.10 \text{ for } h = 0.71)$$

(we assume a weak dependence of f_b on mass from Bialek et al. consistent with observations)

Results at $z=0$

Voevodkin & Vikhlinin (*astro-ph/0305549*)



- Normalization of $F(M)$ at $M_b = 1.0 \times 10^{14} M_\odot$ constrains σ_8 as a function of Ω_M :

$$\sigma_8 = 0.75 \pm 0.04 \text{ for } \Omega_M = 0.3$$