Cooling flows are regions where the importance of non-thermal intracluster medium components such as magnetic fields and cosmic rays may be strongest within a galaxy cluster. They are also regions where such components are best detectable due to the high gas density which influences Faraday rotation measurements of magnetic fields and secondary particle production in hadronic interactions of cosmic ray nuclei with the ambient thermal gas. New estimates of magnetic fields in cooling flow and non-cooling flow clusters are presented, which are based on a newly developed Fourier analysis of extended Faraday rotation maps. We further present new constraints on the cluster cosmic ray proton population using radio and gamma-ray observations of cluster cooling flows, which are especially suited for this purpose due to their high gas and magnetic energy densities. We argue that radio synchrotron emission of cosmic ray electrons generated hadronically by cosmic ray protons is a very plausible explanation for the radio mini-halos observed in some cooling flows.

1. Cooling Flows as a Window to Non-Thermal Intracluster Medium Components

Cooling flows (CFs) are especially well suited places to find traces of otherwise nearly invisible non-thermal components of the intracluster medium (ICM) due to the extreme gas densities observed in CF regions. The faded and therefore invisible remnants of radio galaxy cocoons, so-called radio ghosts (Enßlin 1999) or ghost cavities, were first detected in CFs by the absence of X-ray emissivity in the ghost’s volume in contrast to the highly X-ray luminous cooling flow gas surrounding it (Böhringer et al. 1993; Fabian et al. 2000, and many recent Chandra observations). ICM magnetic fields reveal their presence prominently in CFs by extreme Faraday rotation measures. Cosmic ray electrons (CRe) are seen in CFs by their radio synchrotron radiation in the strong CF magnetic fields. Cosmic ray protons (CRp) in the ICM are most likely to be detected for the first time within CFs via their hadronic interaction with the dense CF gas leading to gamma-rays and CRe.

A better knowledge of these non-thermal components of the ICM—especially in the CF regions—is highly desirable, since they play important roles in the heat balance of the gas through heating by CRp, radio ghost buoyant movements, and suppression of heat conduction by magnetic fields. Additionally, such non-thermal components are tracers of the violent dynamics of the ICM and may help to solve some of the puzzles about CFs.

In this article, we present our recent progress in measuring cluster magnetic fields (Sect. 2) and cosmic ray protons (Sect. 3) in cooling flows. We focus on ideas and results, leaving the technical details to the publications given in the reference list.

2. Faraday Rotation & Magnetic Fields

2.1. Source Intrinsic or External?

The Faraday rotation effect arises whenever polarized radio waves traverse the magnetized ICM which leads to a rotation of the position angle of polarization. This effect allows the measurement of the (electron density weighted) line-of-sight component of cluster magnetic fields. Due to projection, it is not clear where between the radio emitting volume (typically a radio galaxy cocoon) and the observer the Faraday rotation occurs (see Fig. 1).

In order to test if the Faraday rotation is produced in a mixing layer between the radio galaxy cocoon and its surrounding ICM, Rudnick & Blundell (2003) compared rotation measure (RM) maps with intrinsic polarization position angle (PA) maps of the same radio source. The PA is parallel to the source intrinsic magnetic fields and should be uncorrelated to the RM if the Faraday rotation is produced by a source external magnetic field. Therefore, any real co-spatial structures in RM and PA maps would be a very strong indicator of an RM originating from a mixing layer, since only then an RM signature correlated to the PA could be produced. Rudnick & Blundell (2003) tested for such co-spatial structures by measuring the clustering in RM-PA scatter plots and claimed to have found a significant correlation in the RM and PA maps of a radio galaxy.

However, it was shown by Enßlin et al. (2003) that strong clustering in RM-PA scatter plots appears whenever the RM and PA maps have patchy structures independently if the maps are correlated or fully uncorrelated. Such patchy structures are also observed for the maps analyzed by Rudnick & Blundell (2003). In order to test without bias for potential co-spatial RM and
PA structures, Enßlin et al. (2003) developed a method which relies on the alignment of gradients in the PA and RM maps in a sample of radio galaxy datasets. No large-scale gradient alignments could be measured. However, a small-scale gradient alignment is present in all maps. Using a suitable additional test, it could be shown that this alignment signal is a residual of correlated imperfections arising in the RM and PA map making process. Such imperfections produce anti-parallel RM and PA gradients – as found to be responsible for the full small-scale alignment signal – whereas real co-spatial structures should produce parallel and anti-parallel gradients with the same probability.

Therefore, currently no evidence exists for Faraday rotation being local to the source. Independently, there is evidence for relatively strong external magnetic fields by diffuse magneto-synchrotron emission from galaxy clusters observed as radio halos and radio relics. Furthermore, an RM dispersion excess is detected for background radio sources seen through galaxy clusters when compared to control samples (Clarke et al. 2001, and these proceedings). Additionally, given the Laing-Garrington effect (Laing 1988; Garrington et al. 1988), we conclude that the assumption of RM being produced in the foreground ICM of cluster radio sources is strongly favored. We will adopt this point of view in the remainder of this article.

2.2. Statistical Analysis of RM Maps

A sketch of the typical geometry in which magnetic fields are measured from Faraday rotation maps is given in Fig. 2. The cluster magnetic field is sampled in a volume—the sampling window function (or window for short)—which is shaped by the geometry of the used radio source and the gas distribution of the cluster observed (Enßlin & Vogt 2003). If the window is sufficiently extended, the ICM magnetic field can be regarded to be sampled statistically. This may allow the use of statistical methods to restore some of the information lost by the projection of the fields into the RM map.

A crucial piece of information for the measurement of magnetic fields from RM maps is the magnetic autocorrelation length $\lambda_B$. If this is known, the central magnetic field strength of the cluster would simply follow from

\[ \langle B^2 \rangle = \frac{2 \langle RM^2 \rangle}{a_0^2 \bar{n}_e L \lambda_B}, \]

where $\langle RM^2 \rangle$ is the RM dispersion, $L$ is the depth of the Faraday screen, which is well defined in terms of the window function (Enßlin & Vogt 2003), $a_0 = c^3/(2\pi m_e^2 e^4)$, and $n_e$ is the (central) electron density. Here, it is assumed that the magnetic fields are distributed isotropically, so that the observed line-of-sight magnetic field component is representative also for the other two components.

Unfortunately, the magnetic autocorrelation length $\lambda_B$ is not directly accessible. However, the RM autocorrelation length $\lambda_{\text{RM}}$ of the RM maps is easily measurable. Although these length scales are often assumed to be equal in the literature, they are two distinct quantities which usually differ. Under typical circumstances $\lambda_{\text{RM}}$ is expected to exceed $\lambda_B$. The reason for this is that RM maps are more sensitive to large-scale magnetic structures than to small-scale structures, since the latter’s imprint on the RM maps suffers from stronger canceling effects due to field reversals along the line-of-sight. Therefore, inserting $\lambda_{\text{RM}}$ instead of $\lambda_B$ into Eq. 1 should lead to an underestimation of the real magnetic field strength.

An approach to circumvent these difficulties is derived by Enßlin & Vogt (2003): under the assumption of a sufficiently large window, and statistically isotropic magnetic fields with vanishing divergence, it can be shown that the 2-dimensional power spectrum of RM maps is identical to the 3-dimensional magnetic field power spectrum up to a window function dependent (and therefore known) con-
energy density can be calculated. Scales are derived by integrating up to the beam size. The estimates of magnetic field strength and length scales are marked. The estimates of magnetic field strength and length scales are derived by integrating up to the k-vector corresponding to the beam size.

**2.3. Confronting Theory with Data**

The theoretical formalism of Enßlin & Vogt (2003) was applied to an RM map of the north lobe of Hydra A by Vogt & Enßlin (2003). This polarized radio source is embedded in the Hydra cluster cooling flow region. The window function was modeled using up-to-date electron density profiles of the Hydra cluster from X-ray observations. It was assumed that the northern radio cocoon points towards the observer with an angle of $45^\circ$, consistent with the Laing-Garrington effect observed for this source (Taylor & Perley 1993). The resulting power spectrum is shown in Fig. 3. The cluster central magnetic fields are estimated to have a typical field strength of 12 μG, if one integrates this power spectrum up to the Fourier k-vector corresponding to the observational resolution (beam size). As predicted, the magnetic autocorrelation length is significantly shorter than the RM autocorrelation length: $\lambda_B = 0.9$ kpc compared to $\lambda_{RM} = 2$ kpc. If $\lambda_{RM}$ had been used instead of $\lambda_B$ the typical magnetic energy density would have been underestimated by more than a factor of two.

One is tempted to measure the spectral slope of the magnetic power spectrum $\varepsilon_B(k)$ by Fourier transforming RM maps. From the magnetic power spectrum, $\lambda_B$ and the average (cluster central) magnetic field, the energy density can be calculated.

The results of such calculations are displayed in Fig. 4. The response to magnetic power on large Fourier scales, and therefore to small-scale spatial power, resembles the delta-function. However, magnetic large-scale power is strongly redistributed over the full Fourier space. Since the large-scale power dominates the total power, the intrinsic spectrum of the magnetic fields in the Hydra A cluster is masked by this effect. Experiments with power-law spectra observed through the window reveal that the observational data is consistent with Kolmogorov-like or steeper spectra.

The redistribution of power in Fourier space affects the accuracy of magnetic field estimates. Since the estimated magnetic field strengths are an integral quantity of the power spectra, the redistribution of power within the Fourier space typically introduces only a moderate error. Magnetic field estimates seem to be robust to this effect, at least on the few 10% accuracy level.

**2.4. Improving Data: Pacman**

Usually, the RM is determined using a least square fit in order to solve $\Phi = RM \lambda^2 + PA$, where $\Phi$ is the measured position angle of polarization at the observed wavelength $\lambda$. However, $\Phi$ is observationally only constrained to values between 0 and $\pi$ leaving the freedom of additions of $\pm n\pi$ (where $n$ is an integer) causing the so called $n\pi$ ambiguity. Therefore, the least square fit has to be applied to all possible $n\pi$-combinations while searching for the $n\pi$-combination for which $\chi^2$ is minimal.

Traditionally, the minimization of $\chi^2$ is done for each data pixel separately. In these RM maps, steps in the RM value from one pixel to the other could be observed. These steps are mostly detected for noisy regions. They seem to be artificial and due to a false solution of the $n\pi$ ambiguity. Enßlin & Vogt (2003) showed that artifacts in the RM map can lead to flattening of the power spectra in their analysis. Thus, magnetic field strength estimates are likely to be overestimated.

In order to determine RM values more reliably, Dolag
et al. (in prep.) suggest to use non-local information to solve the \( n\pi \)-ambiguity. The new \textit{Pacman} algorithm takes advantage of smooth regions in \( \Phi \). For such smooth regions for all observed wavelengths, the RM distribution is expected to be also smooth and is not expected to show jump- or step-like features. Therefore, the solution to the \( n\pi \)-ambiguity can be applied to this whole region. This has the advantage that noisier areas can profit from less noisy areas.

The application of \textit{Pacman} can lead to a drastic decrease of noise in RM maps as can be seen in Fig. 5. In this figure an RM map which is obtained using standard least square fit algorithm is shown on the left side. In comparison, an RM map generated by \textit{Pacman} is exhibited on the right hand side. Already a visual inspection of this figure reveals that the \textit{Pacman} map is smoother than the standard fit map.

If one repeats the analysis described above and derives the magnetic power spectra for the \textit{Pacman} map as shown in Fig. 6, one can see the effect of noise in the RM map. The power spectra for the \textit{Pacman} map is steeper than the standard fit map.

Fig. 5.— A comparison between an RM map obtained using standard least square fit routines on the left to an RM map produced by \textit{Pacman} on the right hand side is shown. A by-eye comparison reveals that the \textit{Pacman} map is smoother.

Fig. 6.— The 1-dimensional power spectra calculated for the \textit{Pacman} map is represented by the solid line in comparison to the dashed line which was derived by analyzing the standard fit RM map. The influence of the map making process is clearly visible. The low energy part of the spectra is populated by secondary CRs, while the high energy part is dominated by primary CRs. The CR population was calculated neglecting synchrotron radiation energy losses. Thus, realistic inverse Compton spectra due to this process will exhibit a lower normalization than displayed here.

3. Hadronic Interactions of Cosmic Ray Protons

3.1. Hadronic Reactions

Approximately once in a Hubble time a cosmic ray proton (CRp) collides inelastically with a nucleon of the ICM gas of non-cooling flow clusters. Within CFs, such collisions are much more frequent due to the higher target densities. Such inelastic proton (p) nucleon (N) collisions hadronically produce secondary particles like relativistic electrons, positrons, neutrinos and gamma-rays according to the following reaction chain:

\[
p + N \rightarrow 2N + \pi^\pm/0
\]

\[
\pi^\pm \rightarrow \mu^\pm + \nu_\mu/\bar{\nu}_\mu \rightarrow e^\pm + \nu_e/\bar{\nu}_e + \nu_\mu + \bar{\nu}_\mu
\]

\[
\pi^0 \rightarrow 2\gamma.
\]

The resulting gamma-rays can be detected directly with current and future gamma-ray telescopes. The relativistic electrons and positrons (summarized as CRe) are visible due to two radiation processes: inverse Compton scattering of background photon fields (mainly the cosmic microwave background, but also starlight photons) and radio synchrotron emission in ICM magnetic fields. Especially the latter process provides a very sensitive observational signature of the presence of CRp in cooling flows not only because of the tremendous collecting area of radio telescopes, but also due to the strong magnetic fields in CFs, as Faraday rotation measurements demonstrate.

3.2. Gamma-Ray Constraints from EGRET

Assuming that the CRp population can be described by a power law distribution in momentum, Pfrommer & Enßlin (2003a) developed an analytical formalism to describe the secondary emission spectra from hadronic
CRp interactions which exhibit the simplicity of textbook formulae. This formalism was applied to a sample of nearby X-ray luminous galaxy clusters which are also believed to be powerful gamma ray emitters owing to the present high target densities. Synthetic gamma-ray spectra of the Perseus cooling flow cluster calculated using this formalism are shown in Fig. 7. Assuming that the CRp population follows the spatial distribution of the thermal ambient intracluster gas, we can define the CRp scaling ratio

$$X_{\text{CRp}} = \frac{\varepsilon_{\text{CRp}}}{\varepsilon_{\text{th}}}.$$  \hspace{1cm} (2)

The parent CRp spectra giving rise to the hadronically induced gamma-ray spectra are normalized to upper limits on the gamma-ray emission obtained by EGRET observations for energies $E_{\gamma} > 100$ MeV. For nearby CF clusters, this analysis constrains CRp energy densities relative to the thermal energy density to $X_{\text{CRp}} \sim 10\%$. The real gamma-ray spectrum of Perseus is not expected to be far below these spectra. Many processes like supernova driven galactic winds, structure formation shock waves, radio galaxy activity and in situ turbulent particle acceleration support this expectation. These processes should have produced a CRp population characterized by an energy density relative to the thermal energy density of at least a few percent.

The EGRET gamma-ray observation of Perseus limits the CRp content in the central region to be below $X_{\text{CRp}} \sim 10\%$. For the full sample of nearby X-ray luminous clusters, upper limits of the same order of magnitude were obtained as can be seen in Fig. 8. It is obvious from this compilation that CF clusters are extremely well suited to visualize even small CRp populations.

3.3. Gamma-Rays from the Central CF Region of the Virgo Cluster

Recently the HEGRA collaboration (Aharonian et al. 2003) announced a TeV gamma-ray detection from the giant elliptical galaxy M 87 which is situated at the center of the CF region of the Virgo cluster. Using imaging atmospheric Čerenkov techniques, this gamma-ray detection was obtained at a 4$\sigma$ significance level. On the basis of their limited event statistics, it is inconclusive whether the detected emission originates from a point source or an extended source. Despite testing for eruptive behavior of M 87, no time variation of the TeV gamma-ray flux has been found.

Pfrommer & Enßlin (2003b) applied the previously described analytical formalism (Sect. 3.2) of secondary gamma ray emission spectra resulting from hadronic CRp interactions to the central CF region of the Virgo cluster. While combining the observed TeV gamma-ray emission to EGRET upper limits, they constrain the CRp spectral index $\alpha_{\text{CRp}}^{\text{TeV}} < 2.3$ provided the $\gamma$-ray emission is of hadronic origin and the population is described...
by a single power-law ranging from the GeV to TeV energy regime.

A comparison of the observed to the predicted gamma-ray emissivity profiles is shown in Fig. 9. In order to allow for finite resolution of the Čerenkov telescope, the real profile was convolved with the point spread function (PSF) of the HEGRA instrument. The more optimistic PSF of $\sigma = 0.05^\circ$ for harder gamma-ray spectra being favored by our model as well as the conservative choice of a PSF derived from softer Crab-like spectra are both consistent with the observed data. When considering an aged CRp population which has already suffered from significant Coulomb losses, CRp scaling ratios of the order of $X_{\text{CRp}} \approx 2\%$ are obtained for the innermost region of Virgo within $r_{\perp} = 37.5$ kpc.

Since the emission region is dominated by the giant radio galaxy M 87, other mechanisms like processed radiation of the relativistic outflow or dark matter annihilation could also give rise to the observed gamma ray emission. Nevertheless, the hadronic scenario probes the CRp population within a mixture of the interstellar medium of M 87 and the ICM of the Virgo CF region, yielding either an upper limit or a detection on the CRp population, provided this scenario applies.

3.4. Radio Mini-Halos

An upper limit to the CRp population of $X_{\text{CRp}} \approx 2\%$, which is derived from radio observations of the Perseus galaxy cluster, is displayed in Fig. 10. The radio emissivity of hadronically generated CRe depends on the assumed magnetic field strength. Thus, upper limits on $X_{\text{CRp}}$ rely on the same assumption. However, in the case of strong magnetic fields (above 3 $\mu$G), the dependence of $X_{\text{CRp}}$ on the assumed field strength is very weak, since synchrotron losses dominate in this regime. If radio mini-halos are entirely produced hadronically by CRp then the constraint derived for the Perseus cluster is an actual measurement for $X_{\text{CRp}}$ and not only an upper limit.

The Perseus radio mini-halo at 1.4 GHz is shown in Fig. 10 as observed by Pedlar et al. (1990). The emission due to the relativistic jet has been subtracted to make the extended structure more visible. The spatial extent of the radio mini-halo of 160 $h_{70}^{-1}$ kpc in diameter is too large to be accounted for by synchrotron emission of directly accelerated CRe in structure formation or accretion shocks. Thus one needs to consider other injection processes of CRe into the ICM which are responsible for the observed diffuse radio emission. Besides the reacceleration scenario of mildly relativistic CRe ($\gamma \approx 100–300$) which are accelerated in-situ by turbulent Alven waves (Gitti et al. 2002, and these proceedings), the hadronic injection scenario of CRe is a promising alternative.

Azimuthally averaging the radio emission shown in Fig. 10 yields the radio emissivity profile as displayed in Fig. 11. For comparison, we overlaid synthetic radio surface brightness profiles resulting from the hadronic scenario. There is a perfect morphological match between observed and predicted profiles. Alongside the comparably small number of CRp required to account for the observed radio mini-halo, this suggests a hadronic origin of the radio mini-halo in Perseus.

4. Non-thermal conclusions

Our results on magnetic fields and cosmic rays in galaxy cluster cooling flows can be summarized as follows:

Magnetic fields in cooling flows

- Sophisticated statistical tests on Faraday rotation maps as suggested by Rudnick & Blundell (2003) reveal no indications that the Faraday effect occurs in the vicinity of the polarized radio source.
observed (Enßlin et al. 2003). Additionally, several independent pieces of evidence in favor of strong intrachuster magnetic fields lead us therefore to believe that the Faraday rotation signal is due to intrachuster fields, and that the effect is not generated in a hypothetical mixing layer surrounding the observed radio source.

- Faraday rotation measure maps provide a window through which we get a glimpse on the turbulent magnetized intrachuster medium. However, they give us only a projected and partial view of the cluster magnetic field configuration. Therefore statistical methods have to be used to decipher the Faraday signal in terms of magnetic field properties.

- The magnetic field strength derived from the dispersion of rotation measure values depends critically—besides geometrical factors of the galaxy cluster—on the magnetic autocorrelation length, which is not identical to and usually shorter than the autocorrelation length of the rotation measure fluctuations. However, both can be measured from such maps with a novel analysis method (Enßlin & Vogt 2003).

- An application of the novel analysis method of Faraday rotation map to data of a Hydra A reveals magnetic fields $\sim 12 \mu G$ in the center of the cooling flow of the Hydra cluster (Vogt & Enßlin 2003). The magnetic autocorrelation length is 0.9 kpc, and therefore shorter than the rotation measure autocorrelation length of 2.0 kpc, as expected. The magnetic power spectrum is consistent with a Kolmogorov-like or steeper spectrum.

- The small-scale fluctuations in the Faraday rotation map of Hydra A are dominated by noise. The southern maps reveal several step-function-like artifacts, which are probably due to the ambiguity in the absolute polarization angle used to determine the rotation measure. In order to improve the map quality a new map generating algorithm is currently being developed—Pacman—which uses non-local information in order to solve angle ambiguities and which uses improved fitting methods. A preliminary version of Pacman produces maps with strongly reduced noise level.

### Cosmic ray protons in cooling flows

- We argue that cooling flows of galaxy clusters are well suited to reveal or constrain any cosmic ray proton population via radiation from hadronic interactions with the ambient gas nuclei. Such collisions lead to gamma-rays and cosmic ray electrons. The former would have been seen above 100 MeV by the EGRET telescope if the cosmic ray protons had energy densities relative to the thermal gas exceeding 10% (Pfrommer & Enßlin 2003a).

- The giant elliptical galaxy M 87 in the center of the Virgo cluster cooling flow region has recently been detected at TeV energies by the HEGRA instrument (Aharonian et al. 2003). These gamma-rays could be produced by hadronic interactions of a cosmic ray proton population if its spectral index $\alpha_{\text{TeV}} < 2.3$ and its energy density is of the order of 50% of the gas within the transition/mixture of interstellar and intrachuster medium within M 87 (Pfrommer & Enßlin 2003b).

- Cosmic ray electrons produced in hadronic interactions are a very sensitive indicator of cosmic ray protons due to their strong emissivity. Radio synchrotron emission of such electrons in strong cooling flow magnetic fields of $\sim 10 \mu G$ limit the cosmic ray proton energy density to $\sim 2\%$ or less compared to the thermal one in the Perseus cluster cooling flow (Pfrommer & Enßlin 2003a).

- Diffuse radio emission from the Perseus cluster cooling flow was detected—the so called Perseus radio mini-halo. This radio synchrotron emission may be induced by CRp interactions in the ICM. This scenario is strongly supported by the very moderate energy requirements ($2\%$ of the thermal energy) and the excellent agreement between the observed and the theoretically predicted radio surface profile (Pfrommer & Enßlin 2003a).

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